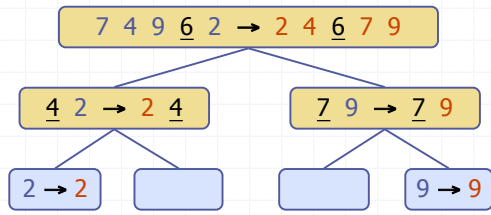
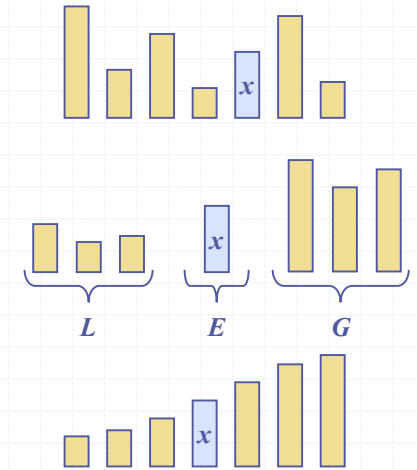


Quick-Sort

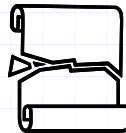


Quick-Sort (§ 10.2)

- ◆ Quick-sort is a randomized sorting algorithm based on the divide-and-conquer paradigm:
 - **Divide:** pick a random element x (called **pivot**) and partition S into
 - ◆ L elements less than x
 - ◆ E elements equal to x
 - ◆ G elements greater than x
 - **Recur:** sort L and G
 - **Conquer:** join L , E and G



Partition



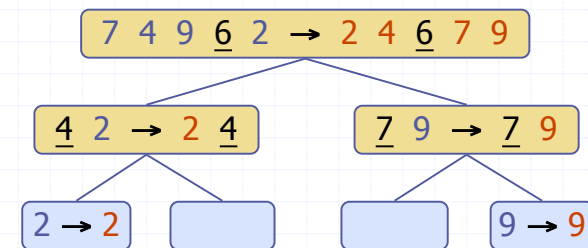
- ◆ We partition an input sequence as follows:
 - We remove, in turn, each element y from S and
 - We insert y into L , E or G , depending on the result of the comparison with the pivot x
- ◆ Each insertion and removal is at the beginning or at the end of a sequence, and hence takes $O(1)$ time
- ◆ Thus, the partition step of quick-sort takes $O(n)$ time

```

Algorithm partition( $S, p$ )
  Input sequence  $S$ , position  $p$  of pivot
  Output subsequences  $L, E, G$  of the
    elements of  $S$  less than, equal to,
    or greater than the pivot, resp.
   $L, E, G \leftarrow$  empty sequences
   $x \leftarrow S.remove(p)$ 
  while  $\neg S.isEmpty()$ 
     $y \leftarrow S.remove(S.first())$ 
    if  $y < x$ 
       $L.insertLast(y)$ 
    else if  $y = x$ 
       $E.insertLast(y)$ 
    else  $\{ y > x \}$ 
       $G.insertLast(y)$ 
  return  $L, E, G$ 
    
```

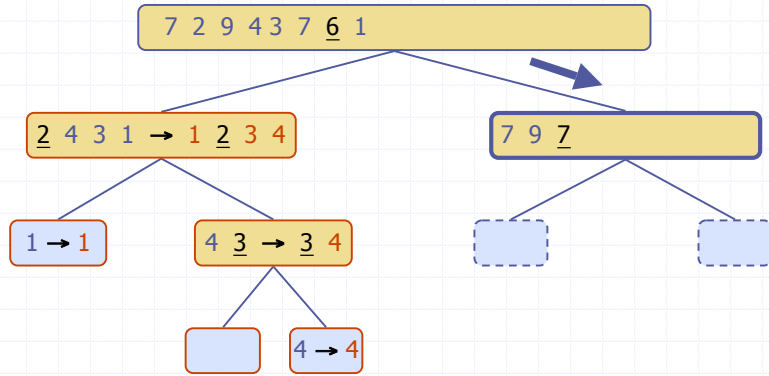
Quick-Sort Tree

- ◆ An execution of quick-sort is depicted by a binary tree
 - Each node represents a recursive call of quick-sort and stores
 - ◆ Unsorted sequence before the execution and its pivot
 - ◆ Sorted sequence at the end of the execution
 - The root is the initial call
 - The leaves are calls on subsequences of size 0 or 1



Execution Example (cont.)

◆ Recursive call, pivot selection



Execution Example (cont.)

◆ Join, join

