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- → Verifying C by translating into Simpl
- → Expressions
- → C control flow
- → Exceptions with Hoare logic rules
- → C functions and procedures with Hoare logic rules

# С

### Main new problems in verifying C programs:

- → expressions with side effects
- → more control flow (do/while, for, break, continue, return)
- → local variables and blocks
- → functions & procedures
- → prevent undefined execution
- → concrete C data types
- → C memory model and C pointers



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# Undefined Execution

In C, we're not allowed to:

- → divide by zero
- → shift more than <architecture defined> bits
- → dereference a Null pointer
- ➔ access outside array bounds
- → access unallocated memory
- ightarrow free unallocated memory
- → ...

### Their absence should become proof obligations.

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Simpl Guards	-
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# Syntax:

Guard 'f "'s bexp" "('s,'p,'f) com"

## Semantics:

 $[|\ s \in g; \ \Gamma \ \vdash (c, \mathsf{Normal} \ s) \Rightarrow t |] \Longrightarrow \Gamma \ \vdash (\mathsf{Guard} \ f \ g \ c, \mathsf{Normal} \ s) \Rightarrow t$ 

 $s \notin g \Longrightarrow \Gamma \vdash (\mathsf{Guard} \ f \ g \ c, \mathsf{Normal} \ s) \Rightarrow Fault f$ 

### Hoare rules:

$\Gamma \vdash_F \{g \land P\} \ c \ \{Q\}$	$f \in F  \Gamma \vdash_F \{g \land P\} \ c \ \{Q\}$
$\Gamma \vdash_F \{g \land P\}$ Guard $f \ g \ c \ Q\}$	$\Gamma \vdash_F \{P\}$ Guard $f \ g \ c \ \{Q\}$

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Simpl Guards: Why two Hoare rules?



### Why two Hoare rules?

So we can separate out verification of guards.

F controls which guards are currently assumed and which are proved.

# Example:

Do automated verification of array guards separately  $\Rightarrow$  get to assume array guards "for free" in the rest.



Simpl Guards: Why two Hoare rules?



## Use Guards for:

Every time an expression or statement does something potentially undefined, add a guard in the translation.

# Example:

 $x = a / b \Rightarrow$  Guard DivByZero (b  $\neq$  0) (x :== a / b)



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Machine Words

Goal: want to write things like

x && y = 0  $\implies$  x + y = x || y

(x << n) !! m = x !! (n + m)

 $x \ll 2 = 4 * x$  ucast (y + 0xFF21) = (x - 0b01001011)

unat x + unat y < 2<sup>^</sup> word\_size  $\implies$  unat (x + y) = unat x + unat y

x :: 32 word y :: 8 word z :: n word

&& bitwise and, || bitwise or, !! test bit at position n, << shift left, "ucast" cast between word sizes, "unat" convert words to nat

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Formalisation Idea	-
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Goal:

Create an Isabelle type that captures machine words of length n

# Problem:

The parameter n is not a type, but a value. This is called a **dependent type**. Isabelle does not support dependent types.

Solutions: make a type 'a word, encode length in type 'a

→ either implicitly as number of elements in 'a,

→ or explicitly via type class function

# Formalisation in Isabelle



### Type class used in HOL/Word/Word.thy:

- → 'a must be class len
- → class len has function len\_of :: 'a itself ⇒ nat
- → to implement class len, a type must provide that function

### 'a itself:

- → 'a itself is a type with one element of type 'a
- → the one element is written TYPE('a)

### Numeric types in Library/Numeral\_Type.thy:

- → create types written as numbers (type 1, 16, etc)
- → have 1, 16, etc elements
- → the numbers are syntax for type constructors encoding 0, 1, 2\*n, 2\*n+1

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### Representation (no taxation)



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Now can encode length. How do we represent words?

### Options:

- → nat mod 2<sup>^</sup> n
- → int mod 2^ n
- → bool lists of length n
- $\clubsuit$  test-bit functions nat  $\Rightarrow$  bool

All of these are equivalent. Actual definition in Isabelle is int mod 2<sup>^</sup> n.

All others are provided as well as simulated type defs.

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### Operators



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### Rest is standard (see HOL/Word/Word.thy + HOL/Word/Examples/):

- → define standard arithmetic and bit-wise operators with syntax
- → prove lemmas connecting to known type representations
- → determine abstract structure:
- commutative ring with 1, partial order, boolean algebra for bitwise ops, etc

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- → prove library with characteristic properties
- → provide some automation: smt connection, auto cast to nat
- → ...
- → profit

# C Data types



### Can now represent all C types apart from float.

(Making explicit architecture assumptions on size etc.)

- → integer types (incl enum): word
- → pointers: datatype 'a ptr = 32 word
- → arrays: pointers or array types in Isabelle
- → structs: records or data types
- → unions: separate struct types with conversions
- → function pointers: word

### Missing: modelling C memory

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# C Memory Model



### Heap models so far:

- → addr ⇒ obj option
- → separate heaps by type
- → separate heaps by record field

# C is more ugly:

- → pointer arithmetic and casting breaks type safety
- → objects could overlap
- → objects can be access under different types (union)
- → systems programmers might rely on data layout (device access)
- → could have pointers into stack (reference to local var)

Our model solves all but the last one.

(Can also solve that one, but it gets even more ugly.)

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**DEMO: WORD** 

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# C Memory Model

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## The Memory Model:

Heap = function "32 word  $\Rightarrow$  8 word"

# That it's.

Ok, not quite: It's the basis. We build a whole machinery on top.

# Basic idea:

- $\clubsuit$  32 word  $\Rightarrow$  8 word is the information that C runtime has
- → we store additional type information for proofs (ghost state)
- → use that type information to automatically get abstract Isabelle objects from heap
- → if we stay in type-safe fragment of C, can reason like in separate heaps.



C Memory Model Diagram (2)

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- → basic function "32 word  $\Rightarrow$  8 word"
- → additional type information for regions of memory



# Encoding Type Information



32A07F10

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### Another type class:

- → for Isabelle types 'a that represent C types
- → from-bytes :: 8 word list  $\Rightarrow$  'a option
- $\clubsuit$  to-bytes :: 'a  $\Rightarrow$  8 word list
- $\clubsuit$  size-of :: 'a itself  $\Rightarrow$  nat
- → tag :: 'a itself  $\Rightarrow$  typ-tag

# Laws:

- → from-bytes (to-bytes v) = Some v
- → length (to-bytes (v::'a)) = size-of TYPE('a)

Example picture unsigned int = 32 word (depending on architecture):

- → from-bytes/to-bytes = big/little endian encoding (depending on architecture)
- → size-of = 4
- → tag = "32 word"

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size-of TYPE (int)

7F 10 32 A0



# Separate Heaps



# Plan:

→ combine type info and real heap into one object typed-hp

- → write 'view' function lift :: typed-hp  $\Rightarrow$  ('a ptr  $\Rightarrow$  'a option)
- → models type-safe heap access
- → returns None if request type 'a does not match type in memory

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