

COMP 4161 NICTA Advanced Course

Advanced Topics in Software Verification

Gerwin Klein, June Andronick, Toby Murray, Christine Rizkallah

$$\{\mathsf{P}\}\ldots\{\mathsf{Q}\}$$

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Last Time



- → Syntax of a simple imperative language
- ➔ Operational semantics
- ➔ Program proof on operational semantics
- ➔ Hoare logic rules
- → Soundness of Hoare logic

Content

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Intro & motivation, getting started	[1]
 Foundations & Principles Lambda Calculus, natural deduction Higher Order Logic Term rewriting 	[1,2] [3ª] [4]
 Proof & Specification Techniques Inductively defined sets, rule induction Datatypes, recursion, induction Hoare logic, proofs about programs, C verification (mid-semester break) Writing Automated Proof Methods Isar, codegen, typeclasses, locales 	[5] [6, 7] [8 ^b ,9] [10] [11 ^c ,12]
	Intro & motivation, getting started Foundations & Principles • Lambda Calculus, natural deduction • Higher Order Logic • Term rewriting Proof & Specification Techniques • Inductively defined sets, rule induction • Datatypes, recursion, induction • Hoare logic, proofs about programs, C verification • (mid-semester break) • Writing Automated Proof Methods • Isar, codegen, typeclasses, locales

^aa1 due; ^ba2 due; ^ca3 due

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Last time: Hoare rule application is nicer than using operational semantic.

BUT:

- → it's still kind of tedious
- ➔ it seems boring & mechanical

Automation?



Problem: While - need creativity to find right (invariant) P

Solution:

- → annotate program with invariants
- → then, Hoare rules can be applied automatically

Example:

 $\begin{array}{l} \{M=0 \land N=0\} \\ \text{WHILE } M \neq a \text{ INV } \{N=M*b\} \text{ DO } N:=N+b; M:=M+1 \text{ OD } \\ \{N=a*b\} \end{array}$



pre
$$c Q$$
 = weakest P such that $\{P\} c \{Q\}$

With annotated invariants, easy to get:

pre SKIP Q = Q
pre
$$(x := a) Q$$
 = $\lambda \sigma. Q(\sigma(x := a\sigma))$
pre $(c_1; c_2) Q$ = pre c_1 (pre $c_2 Q$)
pre (IF *b* THEN c_1 ELSE c_2) Q = $\lambda \sigma. (b \longrightarrow \text{pre } c_1 Q \sigma) \land$
 $(\neg b \longrightarrow \text{pre } c_2 Q \sigma)$
pre (WHILE *b* INV / DO *c* OD) Q = *I*



{pre $c \ Q$ } $c \ \{Q\}$ only true under certain conditions

These are called **verification conditions** vc c Q:

vc
$$c \ Q \land (P \Longrightarrow \mathsf{pre} \ c \ Q) \Longrightarrow \{P\} \ c \ \{Q\}$$

Syntax Tricks



- → $x := \lambda \sigma$. 1 instead of x := 1 sucks
- → $\{\lambda\sigma. \sigma x = n\}$ instead of $\{x = n\}$ sucks as well

Problem: program variables are functions, not values

Solution: distinguish program variables syntactically

Choices:

- → declare program variables with each Hoare triple
 - nice, usual syntax
 - works well if you state full program and only use vcg
- → separate program variables from Hoare triple (use extensible records),

indicate usage as function syntactically

- more syntactic overhead
- program pieces compose nicely



Dемо

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Depending on language, model arrays as functions:

➔ Array access = function application:

→ Array update = function update:

a[i] :== v = a :== a(i:= v)

Use lists to express length:

→ Array update = list update:

→ Array length = list length: a.length = length a

Pointers



Choice 1

- → hp :: heap, p :: ref
- → Pointer access: *p = the_Int (hp (the_addr p))
- → Pointer update: *p :== v = hp :== hp ((the_addr p) := v)
- ➔ a bit klunky
- ➔ gets even worse with structs
- → lots of value extraction (the_Int) in spec and program



Choice 2 (Burstall '72, Bornat '00)

Example: struct with next pointer and element

datatype	ref	= Ref int Null
types	next_hp	= int \Rightarrow ref
types	elem₋hp	= int \Rightarrow int

- → next :: next_hp, elem :: elem_hp, p :: ref
- → Pointer access: $p \rightarrow next$ = next (the_addr p)
- → Pointer update: p→next :== v = next :== next ((the_addr p) := v)

In general:

- → a separate heap for each struct field
- → buys you p→next \neq p→elem automatically (aliasing)
- → still assumes type safe language



Dемо

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- → Weakest precondition
- → Verification conditions
- → Example program proofs
- → Arrays, pointers