Introduction to Information Retrieval

Lecture 5: Index Compression

Last lecture – index construction

- Sort-based indexing
 - Naïve in-memory inversion
 - Blocked Sort-Based Indexing
 - Merge sort is effective for disk-based sorting (avoid seeks!)
- Single-Pass In-Memory Indexing
 - No global dictionary
 - Generate separate dictionary for each block
 - Don't sort postings
 - Accumulate postings in postings lists as they occur
- Distributed indexing using MapReduce
- Dynamic indexing: Multiple indices, logarithmic merge

Today



- Collection statistics in more detail (with RCV1)
 - How big will the dictionary and postings be?
- Dictionary compression
- Postings compression

Why compression (in general)?

- Use less disk space
 - Saves a little money
- Keep more stuff in memory
 - Increases speed
- Increase speed of data transfer from disk to memory
 - [read compressed data | decompress] is faster than [read uncompressed data]
 - Premise: Decompression algorithms are fast
 - True of the decompression algorithms we use

Why compression for inverted indexes?

- Dictionary
 - Make it small enough to keep in main memory
 - Make it so small that you can keep some postings lists in main memory too
- Postings file(s)
 - Reduce disk space needed
 - Decrease time needed to read postings lists from disk
 - Large search engines keep a significant part of the postings in memory.
 - Compression lets you keep more in memory
- We will devise various IR-specific compression schemes

Recall Reuters RCV1

	symbol	statistic	value
	Ν	documents	800,000
	L	avg. # tokens per doc	200
	Μ	terms (= word types)	~400,000
1		avg. # bytes per token (incl. spaces/punct.)	6
1		avg. # bytes per token (without spaces/punct.)	4.5
		avg. # bytes per term	7.5
		non-positional postings	100,000,000

Index parameters vs. what we index (details *IIR* Table 5.1, p.80)

size of	word types (terms)			non-positional postings			positional postings		
	dictionary			non-positional index			positional index		
	Size (K)	Δ %	cumul %	Size (K)	$^{\Delta}$ %	cumul %	Size (K)	Δ %	cumul %
Unfiltered	484			109,971			197,879		
No numbers	474	-2	-2	100,680	-8	-8	179,158	-9	-9
Case folding	392	-17	-19	96,969	-3	-12	179,158	0	-9
30 stopwords	391	-0	-19	83,390	-14	-24	121,858	-31	-38
150 stopwords	391	-0	-19	67,002	-30	-39	94,517	-47	-52
stemming	322	-17	-33	63,812	-4	-42	94,517	0	-52

Exercise: give intuitions for all the '0' entries. Why do some zero entries correspond to big deltas in other columns?

Lossless vs. lossy compression

- Lossless compression: All information is preserved.
 - What we mostly do in IR.
- Lossy compression: Discard some information
- Several of the preprocessing steps can be viewed as lossy compression: case folding, stop words, stemming, number elimination.
- Chap/Lecture 7: Prune postings entries that are unlikely to turn up in the top k list for any query.
 - Almost no loss quality for top k list.

Vocabulary vs. collection size

- How big is the term vocabulary?
 - That is, how many distinct words are there?
- Can we assume an upper bound?
 - Not really: At least 70²⁰ = 10³⁷ different words of length 20
- In practice, the vocabulary will keep growing with the collection size
 - Especially with Unicode ③

Vocabulary vs. collection size

- Heaps' law: $M = kT^b$
- M is the size of the vocabulary, T is the number of tokens in the collection
- Typical values: $30 \le k \le 100$ and $b \approx 0.5$
- In a log-log plot of vocabulary size M vs. T, Heaps' law predicts a line with slope about ½
 - It is the simplest possible relationship between the two in log-log space
 - An empirical finding ("empirical law")

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Heaps' Law

For RCV1, the dashed line

 $\log_{10}M = 0.49 \log_{10}T + 1.64$ is the best least squares fit.

Thus, $M = 10^{1.64}T^{0.49}$ so $k = 10^{1.64} \approx 44$ and b = 0.49.

Good empirical fit for Reuters RCV1 !

For first 1,000,020 tokens, law predicts 38,323 terms; actually, 38,365 terms Fig 5.1 p81



Exercises

- What is the effect of including spelling errors, vs. automatically correcting spelling errors on Heaps' law?
- Compute the vocabulary size M for this scenario:
 - Looking at a collection of web pages, you find that there are 3000 different terms in the first 10,000 tokens and 30,000 different terms in the first 1,000,000 tokens.
 - Assume a search engine indexes a total of 20,000,000,000
 (2 × 10¹⁰) pages, containing 200 tokens on average
 - What is the size of the vocabulary of the indexed collection as predicted by Heaps' law?

Zipf's law

- Heaps' law gives the vocabulary size in collections.
- We also study the relative frequencies of terms.
- In natural language, there are a few very frequent terms and very many very rare terms.
- Zipf's law: The *i*th most frequent term has frequency proportional to 1/*i*.
- $cf_i \propto 1/i = K/i$ where K is a normalizing constant
- cf_i is <u>collection frequency</u>: the number of occurrences of the term t_i in the collection.

Zipf consequences

- If the most frequent term (the) occurs cf₁ times
 - then the second most frequent term (*of*) occurs $cf_1/2$ times
 - the third most frequent term (and) occurs cf₁/3 times ...
- Equivalent: cf_i = K/i where K is a normalizing factor, so
 - log cf_i = log K log i
 - Linear relationship between log cf_i and log i
- Another power law relationship



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Compression

- Now, we will consider compressing the space for the dictionary and postings
 - Basic Boolean index only
 - No study of positional indexes, etc.
 - We will consider compression schemes

DICTIONARY COMPRESSION

Why compress the dictionary?

- Search begins with the dictionary
- We want to keep it in memory
- Memory footprint competition with other applications
- Embedded/mobile devices may have very little memory
- Even if the dictionary isn't in memory, we want it to be small for a fast search startup time
- So, compressing the dictionary is important

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Dictionary storage - first cut

Array of fixed-width entries

~400,000 terms; 28 bytes/term = 11.2 MB.



Fixed-width terms are wasteful

- Most of the bytes in the Term column are wasted we allot 20 bytes for 1 letter terms.
 - And we still can't handle *supercalifragilisticexpialidocious* or *hydrochlorofluorocarbons*.
- Written English averages ~4.5 characters/word.
 - Exercise: Why is/isn't this the number to use for estimating the dictionary size?
- Ave. dictionary word in English: ~8 characters
 - How do we use ~8 characters per dictionary term?
- Short words dominate token counts but not type average.

Compressing the term list: Dictionary-as-a-String

Store dictionary as a (long) string of characters: Pointer to next word shows end of current word Hope to save up to 60% of dictionary space.



Space for dictionary as a string

- 4 bytes per term for Freq.
- 4 bytes per term for pointer to Postings.
- 3 bytes per term pointer

```
Now avg. 11
bytes/term,
not 20.
```

- Avg. 8 bytes per term in term string
- 400K terms x 19 → 7.6 MB (against 11.2MB for fixed width)

Blocking

- Store pointers to every kth term string.
 - Example below: *k*=4.
- Need to store term lengths (1 extra byte)



Net

- Example for block size k = 4
- Where we used 3 bytes/pointer without blocking
 - 3 x 4 = 12 bytes,
- now we use 3 + 4 = 7 bytes.

Shaved another ~0.5MB. This reduces the size of the dictionary from 7.6 MB to 7.1 MB. We can save more with larger *k*.

Why not go with larger k?

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Exercise

Estimate the space usage (and savings compared to 7.6 MB) with blocking, for block sizes of k = 4, 8 and 16.

Dictionary search without blocking

 Assuming each dictionary term equally likely in query (not really so in practice!), average number of comparisons = (1+2·2+4·3+4)/8~2.6

Exercise: what if the frequencies of query terms were non-uniform but known, how would you structure the dictionary search tree?



Dictionary search with blocking



- Binary search down to 4-term block;
 - Then linear search through terms in block.
- Blocks of 4 (binary tree), avg. = (1+2·2+2·3+2·4+5)/8 = 3 compares

Exercise

Estimate the impact on search performance (and slowdown compared to k=1) with blocking, for block sizes of k = 4, 8 and 16.

Front coding

Front-coding:

- Sorted words commonly have long common prefix store differences only
- (for last k-1 in a block of k)

8automata8automate9automatic10automation



Begins to resemble general string compression. 29

Front Encoding [Witten, Moffat, Bell]

- Complete front encoding
 - (prefix-len, suffix-len, suffix)
- Partial 3-in-4 front encoding
 - No encoding/compression for the first string in a block
 - Enables binary search

Assume	String	Complete Front Encoding	Partial 3-in-4 Front Encoding		
previous	8, automata	4, 4, mata	, 8, automata		
string is	8, automate	7, 1, e	7, 1, e		
auto	9, automatic	7, 2, ic	7, 2, ic		
	10, automation	8, 2, on	8, , on		

RCV1 dictionary compression summary

Technique	Size in MB
Fixed width	11.2
Dictionary-as-String with pointers to every term	7.6
Also, blocking <i>k</i> = 4	7.1
Also, Blocking + front coding	5.9

POSTINGS COMPRESSION

Postings compression

- The postings file is much larger than the dictionary, factor of at least 10.
- Key desideratum: store each posting compactly.
- A posting for our purposes is a docID.
- For Reuters (800,000 documents), we would use 32 bits per docID when using 4-byte integers.
- Alternatively, we can use log₂ 800,000 ≈ 20 bits per docID.
- Our goal: use a lot less than 20 bits per docID.

Postings: two conflicting forces

- A term like *arachnocentric* occurs in maybe one doc out of a million – we would like to store this posting using log₂ 1M ~ 20 bits.
- A term like *the* occurs in virtually every doc, so 20 bits/posting is too expensive.
 - Prefer 0/1 bitmap vector in this case

Postings file entry

- We store the list of docs containing a term in increasing order of docID.
 - *computer*: 33,47,154,159,202 ...
- <u>Consequence</u>: it suffices to store *gaps*.
 - **3**3,14,107,5,43 ...
- <u>Hope</u>: most gaps can be encoded/stored with far fewer than 20 bits.

Three postings entries

	encoding	postings	list								
THE	docIDs			283042		283043		283044		283045	
	gaps				1		1		1		
COMPUTER	docIDs			283047		283154		283159		283202	
	gaps				107		5		43		
ARACHNOCENTRIC	docIDs	252000		500100							
	gaps	252000	248100								

Variable length encoding

- Aim:
 - For *arachnocentric*, we will use ~20 bits/gap entry.
 - For *the*, we will use ~1 bit/gap entry.
- If the average gap for a term is G, we want to use ~log₂G bits/gap entry.
- <u>Key challenge</u>: encode every integer (gap) with about as few bits as needed for that integer.
- This requires a variable length encoding
- Variable length codes achieve this by using short codes for small numbers

Variable Byte (VB) codes

- For a gap value G, we want to use close to the fewest bytes needed to hold log₂ G bits
- Begin with one byte to store G and dedicate 1 bit in it to be a <u>continuation bit</u> c
- If G ≤127, binary-encode it in the 7 available bits and set c =1
- Else encode G's lower-order 7 bits and then use additional bytes to encode the higher order bits using the same algorithm
- At the end set the continuation bit of the last byte to
 1 (c = 1) and for the other bytes c = 0.

Hex(824)=0x0338 Hex(214577)=0x00034631

Example

0x0338 = (0000 0011 0011 1000)



For a small gap (5), VB uses a whole byte. ³⁹

Byte-Aligned Variable-length Encodings

- Varint encoding:
 - -7 bits per byte with continuation bit
 - Con: Decoding requires lots of branches/shifts/masks





Byte-Aligned Variable-length Encodings

- Varint encoding:
 - -7 bits per byte with continuation bit
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- Idea: Encode byte length using 2 bits
 - Better: fewer branches, shifts, and masks
 - Con: Limited to 30-bit values, still some shifting to decode



Group Varint Encoding

- Idea: encode groups of 4 32-bit values in 5-17 bytes
 - Pull out 4 2-bit binary lengths into single byte prefix



• Decode: Load prefix byte and use value to lookup in 256-entry table:

00000110 ---- Offsets: +1,+2,+3,+5; Masks: ff, ff, ffff, ffffff

- Much faster than alternatives:
 - 7-bit-per-byte varint: decode ~180M numbers/second
 - 30-bit Varint w/ 2-bit length: decode ~240M numbers/second
 - Group varint: decode ~400M numbers/second

Other variable unit codes

- Instead of bytes, we can also use a different "unit of alignment": 32 bits (words), 16 bits, 4 bits (nibbles).
- Variable byte alignment wastes space if you have many small gaps – nibbles do better in such cases.
- Variable byte codes:
 - Used by many commercial/research systems
 - Good low-tech blend of variable-length coding and sensitivity to computer memory alignment matches (vs. bit-level codes, which we look at next).
- There is also recent work on word-aligned codes that pack a variable number of gaps into one word (e.g., simple9)

Simple9

- Encodes as many gaps as possible in one DWORD
- 4 bit selector + 28 bit data bits
 - Encodes 9 possible ways to "use" the data bits

Selector	# of gaps encoded	Len of each gap encoded	Wasted bits
0000	28	1	0
0001	14	2	0
0010	9	3	1
0011	7	4	0
0100	5	5	3
0101	4	7	0
0110	3	9	1
0111	2	14	0
1000	1	28	0

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Unary code

- Represent n as n 1s with a final 0.
- Unary code for 3 is 1110.
- Unary code for 80 is:

This doesn't look promising, but....

Bit-Aligned Codes

- Breaks between encoded numbers can occur after any bit position
- Unary code
 - Encode k by k 1s followed by 0
 - 0 at end makes code unambiguous

Number	Code
0	0
1	10
2	110
3	1110
4	11110
5	111110

Unary and Binary Codes

- Unary is very efficient for small numbers such as 0 and 1, but quickly becomes very expensive
 - 1023 can be represented in 10 binary bits, but requires 1024 bits in unary
- Binary is more efficient for large numbers, but it may be ambiguous

Elias-y Code

To encode a number k, compute

- $k_d = \lfloor \log_2 k \rfloor$ unary • $k_r = k - 2^{\lfloor \log_2 k \rfloor}$ binary
- *k_d* is number of binary digits, encoded in unary

Number (k)	k_d	k_r	Code
1	0	0	0
2	1	0	10 0
3	1	1	10 1
6	2	2	110 10
15	3	7	1110 111
16	4	0	$11110 \ 0000$
255	7	127	$11111110 \ 1111111$
1023	9	511	1111111110 111111111

Elias-δ Code

- Elias-γ code uses no more bits than unary, many fewer for k > 2
 - 1023 takes 19 bits instead of 1024 bits using unary
- In general, takes 2Llog₂kl+1 bits
- To improve coding of large numbers, use Elias-δ code
 - Instead of encoding k_d in unary, we encode k_d + 1 using Elias-γ
 - Takes approximately 2 log₂ log₂ k + log₂ k bits

Elias-δ Code

Split (*k_d*+ 1) into:

$$k_{dd} = \lfloor \log_2(k_d + 1) \rfloor$$
$$k_{dr} = (k_d + 1) - 2^{\lfloor \log_2(k_d + 1) \rfloor}$$

• encode k_{dd} in unary, k_{dr} in binary, and k_r in binary

Number (k)	$ k_d $	k_r	k_{dd}	k_{dr}	Code
1	0	0	0	0	0
2	1	0	1	0	10 0 0
3	1	1	1	0	$10 \ 0 \ 1$
6	2	2	1	1	10 1 10
15	3	7	2	0	$110 \ 00 \ 111$
16	4	0	2	1	$110\ 01\ 0000$
255	7	127	3	0	$1110\ 000\ 1111111$
1023	9	511	3	2	$1110\ 010\ 111111111$

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```
# Generating Elias-gamma and Elias-delta codes in Python
#
import math
def unary_encode(n):
 return "1" * n + "0"
def binary_encode(n, width):
    r = ""
    for i in range(0,width):
     if ((1<<i) & n) > 0:
     r = "1" + r
     else:
     r = "0" + r
    return r
def gamma_encode(n):
    logn = int(math.log(n,2))
    return unary_encode( logn ) + " " + binary_encode(n, logn)
def delta_encode(n):
 logn = int(math.log(n,2))
if n == 1:
  return "0"
  else:
 loglog = int(math.log(logn+1,2))
 residual = logn+1 - int(math.pow(2, loglog))
        return unary_encode( loglog ) + " " + binary_encode( residual, loglog ) + " " + binary_encode(n, logn)
if __name__ == "__main__":
    for n in [1,2,3, 6, 15,16,255,1023]:
        logn = int(math.log(n,2))
        loglogn = int(math.log(logn+1,2))
        print n, "d_r", logn
        print n, "d_dd", loglogn
        print n, "d_dr", logn + 1 - int(math.pow(2,loglogn))
        print n, "delta", delta_encode(n)
        #print n, "gamma", gamma_encode(n)
        #print n, "binary", binary_encode(n)
```

Gamma code properties

- G is encoded using $2 \log G + 1$ bits
 - Length of offset is log G bits
 - Length of length is $\log G + 1$ bits
- All gamma codes have an odd number of bits
- Almost within a factor of 2 of best possible, log₂ G
- Gamma code is uniquely prefix-decodable, like VB
- Gamma code can be used for any distribution
- Gamma code is parameter-free

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Gamma seldom used in practice

- Machines have word boundaries 8, 16, 32, 64 bits
 - Operations that cross word boundaries are slower
- Compressing and manipulating at the granularity of bits can be slow
- Variable byte encoding is aligned and thus potentially more efficient
- Regardless of efficiency, variable byte is conceptually simpler at little additional space cost

Shannon Limit

- Is it possible to derive codes that are optimal (under certain assumptions)?
- What is the optimal average code length for a code that encodes each integer (gap lengths) independently?
- Lower bounds on average code length: Shannon entropy
 - $H(X) = -\Sigma_{x=1}^{n} Pr[X=x] \log Pr[X=x]$
- Asymptotically optimal codes (finite alphabets): arithmetic coding, Huffman codes

RCV1 compression

Data structure	Size in MB
dictionary, fixed-width	11.2
dictionary, term pointers into string	7.6
with blocking, $k = 4$	7.1
with blocking & front coding	5.9
collection (text, xml markup etc)	3,600.0
collection (text)	960.0
Term-doc incidence matrix	40,000.0
postings, uncompressed (32-bit words)	400.0
postings, uncompressed (20 bits)	250.0
postings, variable byte encoded	116.0
postings, γ–encoded	101.0

Google's Indexing Choice

- Index shards partition by doc, multiple replicates
- Disk-resident index
 - Use outer parts of the disk
 - Use different compression methods for different fields: Rice_k (a special kind of Golomb code) for gaps, and Gamma for positions.
- In-memory index
 - All positions; No docid
 - Keep track of document boundaries
 - Group-variant encoding
 - Fast to decode

Source: Jeff Dean's WSDM 2009 Keynote

Other details

- Gap = docid_n- docid_{n-1} 1
- Freq = freq -1
- $Pos_Gap = pos_n pos_{n-1} 1$
- C.f., Jiangong Zhang, Xiaohui Long and Torsten Suel: Performance of Compressed Inverted List Caching in Search Engines. WWW 2008.

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Index compression summary

- We can now create an index for highly efficient Boolean retrieval that is very space efficient
- Only 4% of the total size of the collection
- Only 10-15% of the total size of the <u>text</u> in the collection
- However, we've ignored positional information
- Hence, space savings are less for indexes used in practice
 - But techniques substantially the same.

Resources for today's lecture

- IIR 5
- *MG* 3.3, 3.4.
- F. Scholer, H.E. Williams and J. Zobel. 2002. Compression of Inverted Indexes For Fast Query Evaluation. *Proc. ACM-SIGIR 2002*.
 - Variable byte codes
- V. N. Anh and A. Moffat. 2005. Inverted Index Compression Using Word-Aligned Binary Codes. *Information Retrieval* 8: 151–166.
 - Word aligned codes