

COMP 4161

NICTA Advanced Course

Advanced Topics in Software Verification

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Content

Content	NICTA
→ Intro & motivation, getting started	[1]
→ Foundations & Principles	
 Lambda Calculus, natural deduction 	[1,2]
Higher Order Logic	[3 ^{<i>a</i>}]
 Term rewriting 	[4]
Proof & Specification Techniques	
 Inductively defined sets, rule induction 	[5]
 Datatypes, recursion, induction 	[6, 7]
 Hoare logic, proofs about programs, C verification 	[8 ^b ,9]
 (mid-semester break) 	
 Writing Automated Proof Methods 	[10]
 Isar, codegen, typeclasses, locales 	[11 ^{<i>c</i>} ,12]

^{*a*}a1 due; ^{*b*}a2 due; ^{*c*}a3 due



Automatic Proof and Disproof

- → Sledgehammer: automatic proofs
- → Quickcheck: counter example by testing
- → Nipick: counter example by SAT

Based on slides by Jasmin Blanchette, Lukas Bulwahn, and Tobias Nipkow (TUM).



Dramatic improvements in fully automated proofs in the last 2 decades.

- → First-order logic (ATP): Otter, Vampire, E, SPASS
- → Propositional logic (SAT): MiniSAT, Chaff, RSat
- → SAT modulo theory (SMT): CVC3, Yices, Z3

The key:

Efficient reasoning engines, and restricted logics.



1980s rule applications, write ML code

1990s simplifier, automatic provers (blast, auto), arithmetic

2000s embrace external tools, but don't trust them (ATP/SMT/SAT)



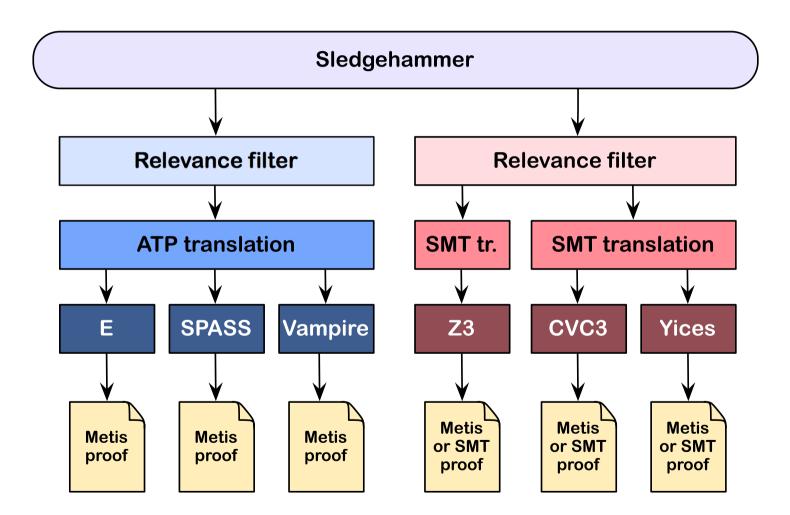
Sledgehammer:

- → Connects Isabelle with ATPs and SMT solvers:
 - E, SPASS, Vampire, CVC3, Yices, Z3
- → Simple invocation:
 - ➔ Users don't need to select or know facts
 - \rightarrow or ensure the problem is first-order
 - → or know anything about the automated prover
- → Exploits local parallelism and remote servers



DEMO: SLEDGEHAMMER

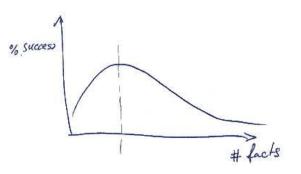






Provers perform poorly if given 1000s of facts.

- → Best number of facts depends on the prover
- → Need to take care which facts we give them
- → Idea: order facts by relevance, give top n to prover (n = 250, 1000, ...)
- → Meng & Paulson method: lightweight, symbol-based filter
- Machine learning method: look at previous proofs to get a probability of relevance





Source: higher-order, polymorphism, type classes **Target:** first-order, untyped or simply-typed

→ First-order:

- → SK combinators, λ -lifting
- → Explicit function application operator

→ Encode types:

- → Monomorphise (generate multiple instances), or
- ➔ Encode polymorphism on term level



We don't want to trust the external provers.

Need to check/reconstruct proof.

- Re-find using Metis
 Usually fast and reliable (sometimes too slow)
- Rerun external prover for trusted replay Used for SMT. Re-runs prover each time!
- → Recheck stored explicit external representation of proof Used for SMT, no need to re-run. Fragile.
- → Recast into structured Isar proof Fast, experimental.

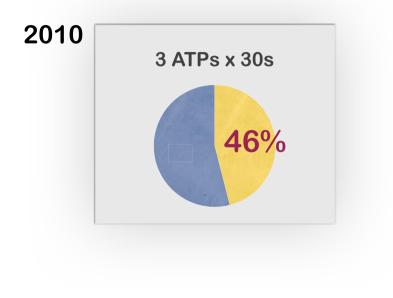


Evaluating Sledgehammer:

- → 1240 goals out of 7 existing theories.
- → How many can sledgehammer solve?
- → 2010: E, SPASS, Vampire (for 5-120s). 46%
 ESV × 5s ≈ V × 120s
- → 2011: Add E-SInE, CVC2, Yices, Z3 (30s).
 Z3 > V
- → 2012: Better integration with SPASS. 64% SPASS best (small margin)
- → 2013: Machine learning for fact selection. 69% Improves a few percent across provers.

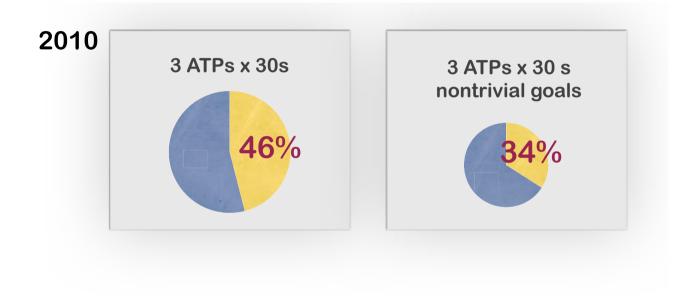
Evaluation





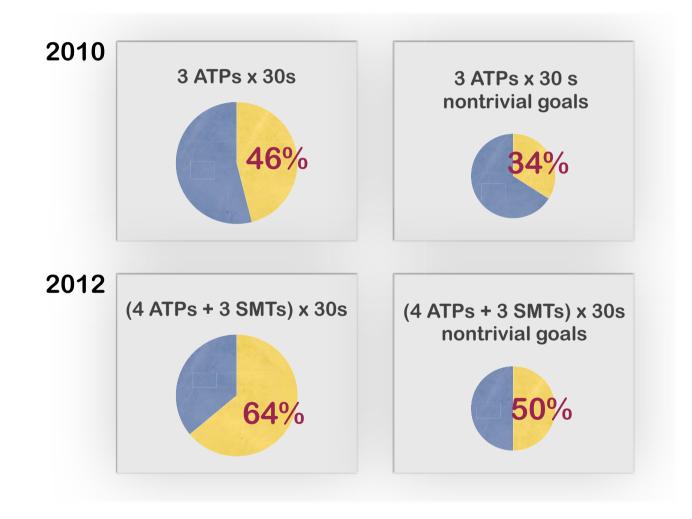
Evaluation





Evaluation







Example application:

- → Large Isabelle/HOL repository of algebras for modelling imperative programs (Kleene Algebra, Hoare logic, ..., ≈ 1000 lemmas)
- ➔ Intricate refinement and termination theorems
- → Sledgehammer and Z3 automate algebraic proofs at textbook level.

"The integration of ATP, SMT, and Nitpick is for our purposes very very helpful." – G. Struth



DISPROOF



Testing can show only the presence of errors, but not their absence. (Dijkstra)

Testing cannot prove theorems, but it can refute conjectures!

Sad facts of life:

- → Most lemma statements are wrong the first time.
- → Theorem proving is expensive as a debugging technique.

Find counter examples automatically!



Lightweight validation by testing.

- ➔ Motivated by Haskell's QuickCheck
- → Uses Isabelle's code generator
- → Fast
- → Runs in background, proves you wrong as you type.



Covers a number of testing approaches:

- → Random and exhausting testing.
- → Smart test data generators.
- → Narrowing-based (symbolic) testing.

Creates test data generators automatically.



DEMO: QUICKCHECK



Fast iteration in continuation-passing-style

datatype α list = Nil | Cons α (α list)

Test function:

test_{α list} P = P Nil andalso test_{α} (λ x. test_{α list} (λ xs. P (Cons x xs)))



distinct $xs \implies$ distinct (remove1 x xs)

Problem:

Exhaustive testing creates many useless test cases.

Solution:

Use definitions in precondition for smarter generator. Only generate cases where *distinct xs* is true.

test-distinct_{α list} P = P Nil *andalso* test_{α} (λ x. test-distinct_{α list} (if x \notin xs then (λ xs. P (Cons x xs)) else True))

Use data flow analysis to figure out which variables must be computed and which generated.



Symbolic execution with demand-driven refinement

- ➔ Test cases can contain variables
- → If execution cannot proceed: instantiate with further symbolic terms

Pays off if large search spaces can be discarded:

distinct (Cons 1 (Cons 1 x))

False for any *x*, no further instantiations for x necessary.

Implementation:

Lazy execution with outer refinement loop. Many re-computations, but fast.



Only executable specifications!

- → No equality on functions with infinite domain
- ➔ No axiomatic specifications



NITPICK



Finite model finder

- → Based on SAT via Kodkod (backend of Alloy prover)
- → Soundly approximates infinite types

Nitpick Successes



- → Algebraic methods
- → C++ memory model
- ➔ Found soundness bugs in TPS and LEO-II

Fan mail:

"Last night I got stuck on a goal I was sure was a theorem. After 5–10 minutes I gave Nitpick a try, and within a few secs it had found a splendid counterexample—despite the mess of locales and type classes in the context!"



DEMO: NITPICK



We have seen today ...

- ➔ Proof: Sledgehammer
- → Counter examples: Quickcheck
- → Counter examples: Nitpick